| 1 |  | mark | notes |
| :---: | :---: | :---: | :---: |
| (i) | $\begin{aligned} & \mathbf{F}=(10-8 \cos 50) \mathbf{i}+8 \sin 50 \mathbf{j} \\ & =4.85769 \ldots \mathbf{i}+6.128355 \ldots \mathbf{j} \\ & \text { so } 4.86 \mathbf{i}+6.13 \mathbf{j}(3 \text { s. f. }) \end{aligned}$ | M1 <br> A1 <br> A1 3 | Resolution. Accept $s \leftrightarrow c$. Condone resolution in only one direction. <br> Award for a vector with either component correct or consistent $s \leftrightarrow c$ error is only mistake in the vector. Need not be evaluated. <br> cao. Must be in $a \mathbf{i}+b \mathbf{j}$ or column format. Must be correct to 3 s. f. |
| (ii) | $\begin{aligned} & \|\mathbf{F}\|=\sqrt{4.85769 \ldots^{2}+6.12835 \ldots{ }^{2}}=7.820101 \ldots \\ & \text { so } 7.82(3 \text { s. f.) } \\ & \text { angle is } \arctan \frac{4.857 \ldots}{6.128 \ldots} \\ & =38.40243 \ldots \text { so } 38.4^{\circ}(3 \text { s. f. }) \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { F1 } \\ & \hline \end{aligned}$ | FT their F <br> Or equivalent. FT their F. Accept $\arctan \frac{6.128 \ldots}{4.857 \ldots}$. Accept complementary angle and $\pm$ signs <br> FT only their $F$. |
|  |  | 6 |  |


| 2 |  | Mark | Comment |  |
| :---: | :---: | :---: | :---: | :---: |
| (i) | Resultant is $\left(\begin{array}{l}4 \\ 1 \\ 2\end{array}\right)+\left(\begin{array}{c}-6 \\ 2 \\ 4\end{array}\right)=\left(\begin{array}{c}-2 \\ 3 \\ 6\end{array}\right)$ <br> Magnitude is $\sqrt{(-2)^{2}+3^{2}+6^{2}}=\sqrt{49}=7 \mathrm{~N}$ | M1 <br> A1 <br> M1 <br> F1 | Adding the vectors. Condone spurious notation. <br> Vector must be in proper form (penalise only once in the paper). Accept clear components. <br> Pythagoras on their 3 component vector. Allow e.g. $-2^{2}$ for $(-2)^{2}$ even if evaluated as - 4 . <br> FT their resultant. | 4 |
| (ii) | $\mathbf{F}+2 \mathbf{G}+\mathbf{H}=\mathbf{0}$ <br> So $\mathbf{H}=-\mathbf{2} \mathbf{G}-\mathbf{F}=-\left(\begin{array}{c}-12 \\ 4 \\ 8\end{array}\right)-\left(\begin{array}{l}4 \\ 1 \\ 2\end{array}\right)$ $=\left(\begin{array}{c} 8 \\ -5 \\ -10 \end{array}\right)$ | M1 <br> A1 <br> A1 | Either $\mathbf{F}+\mathbf{2 G}+\mathbf{H}=\mathbf{0}$ or $\mathbf{F}+2 \mathbf{G}=\mathbf{H}$ <br> Must see attempt at $\mathbf{H}=-2 \mathbf{G}-\mathbf{F}$ <br> cao. Vector must be in proper form (penalise only once in the paper). | 3 |
|  |  | 7 |  |  |


| 3 |  | mark |  | sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $R=m g$ so 49 N | B1 | Equating to weight. Accept $5 g$ (but not $m g$ ) | 1 |
| (ii) |  | B1 <br> B1 | All except $F$ correct (arrows and labels) (Accept $m g$, $W$ etc and no angle). Accept cpts instead of 10N. No extra forces. F clearly marked and labelled | 2 |
| (iii) | $\begin{aligned} & \uparrow \quad R+10 \cos 40-49=0 \\ & R=41.339 \ldots \text { so } 41.3 \mathrm{~N}(3 \mathrm{~s} . \text { f. }) \\ & F=10 \sin 40=6.4278 \ldots \text { so } 6.43 \mathrm{~N}(3 \mathrm{~s} . \mathrm{f} .) \end{aligned}$ | M1 <br> B1 <br> A1 <br> B1 | Resolve vertically. All forces present and 10N resolved <br> Resolution correct and seen in an equation. <br> (Accept <br> $R= \pm 10 \cos 40$ as an equation) <br> Allow -ve if consistent with the diagram. | 4 |
|  |  |  |  | 7 |


| 4 |  | mark |  | sub |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $\downarrow \quad 20+16 \cos 60=28$ | B1 |  | 1 |
| (ii) | either $\rightarrow 16 \sin 60$ <br> Mag $\sqrt{28^{2}+192}=31.2409 \ldots$ <br> so 31.2 N (3 s.f.) <br> or <br> Cos rule $\begin{aligned} & \mathrm{mag}^{2}=16^{2}+20^{2}-2 \times 16 \times 20 \times \cos 120 \\ & 31.2 \mathrm{~N} \text { (3 s. f.) } \end{aligned}$ | B1 <br> M1 <br> F1 <br> M1 <br> A1 <br> A1 | Any form. May be seen in (i). Accept any appropriate equivalent resolution. <br> Use of Pythag with 2 distinct cpts (but not 16 and $\pm 20)$ <br> Allow 34.788... only as FT <br> Must be used with $20 \mathrm{~N}, 16 \mathrm{~N}$ and $60^{\circ}$ or $120^{\circ}$ Correct substitution | 3 |
| (iii) | Magnitude of accn is $15.620 \ldots \mathrm{~m} \mathrm{~s}^{-2}$ so $15.6 \mathrm{~m} \mathrm{~s}^{-2}$ (3 s. f.) <br> angle with 20 N force is $\arctan \left(\frac{16 \sin 60}{28}\right)$ $\text { so } 26.3295 \ldots \text { so } 26.3^{\circ} \text { (3 s. f.) }$ | B1 <br> M1 <br> A1 | Award only for their $F \div 2$ <br> Or equiv. May use force or acceleration. Allow use <br> of sine or cosine rules. FT only $s \leftrightarrow c$ and sign errors. Accept reciprocal of the fraction. cao | 3 |
|  |  |  |  | 7 |


| 5 |  | mark |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $\left(\begin{array}{c} x \\ -7 \\ z \end{array}\right)+\left(\begin{array}{c} 4 \\ y \\ -5 \end{array}\right)+\left(\begin{array}{c} 5 \\ 4 \\ -7 \end{array}\right)=\left(\begin{array}{l} 0 \\ 0 \\ 0 \end{array}\right)$ <br> Equating components gives $x=-9, y=3, z=12$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | [Allow SC $2 / 4$ if $9,-3,-12$ obtained] | 4 |
| (ii) | $\begin{aligned} & \text { We need } \sqrt{5^{2}+4^{2}+(-7)^{2}} \\ & =\sqrt{90} \text { or } 9.48683 \ldots \text { so } 9.49(3 \mathrm{s.f.}) \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Any reasonable accuracy | 2 |
|  | total | 6 |  |  |


| 6 |  | mark |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (i) |  | B1 | Different labels. All forces present with arrows in correct directions. Condone no angles. | 1 |
| (ii) | Using triangle of forces <br> Triangle isosceles so tension in BC is 400 N <br> Tension in BA is $2 \times 400 \times \cos 30=400 \sqrt{3} \mathrm{~N}$ (693 N, (3 s. f.)) | M1 <br> B1 <br> A1 <br> F1 | Attempt at triangle of forces. Ignore angles and arrows. Accept 90, 60, 30 triangle. <br> Triangle, arrows, labels and angles correct <br> cao <br> FT BC only <br> [If resolution used, M1 for 1 equn; M1 for $2^{\text {nd }}$ equn + attempt to elim; A1; F1. For M marks all forces present but allow $s \leftrightarrow c$ and sign errors. No extra forces. If Lami used: <br> M1 first pair of equations in correct format, condone wrong angles. A1. M1 second pair in correct format, with correct angles.F1 FT their first answer if necessary.] |  |
| (iii) | Resolve at B perpendicular to the line ABC <br> Weight has unbalanced component in this direction | E1 <br> E1 | Attempt to argue unbalanced force <br> Complete, convincing argument. <br> [or Resolve horiz and establish tensions equal E1 Resolve vert to show inconsistency. E1] | 2 |
|  | total | 7 |  |  |

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